

# **Simulating Thermal Transport in Nanostructures from the Ballistic to the Diffusive Regime**

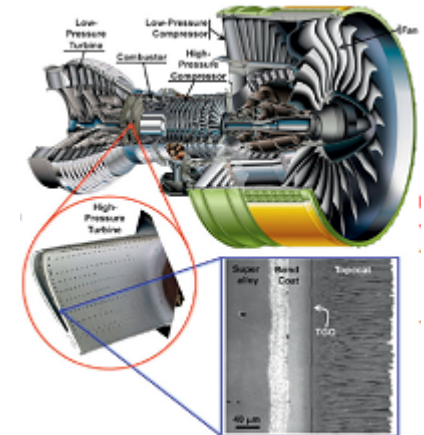
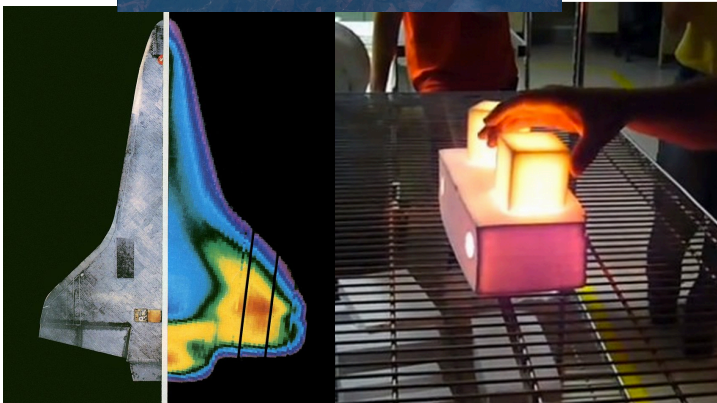
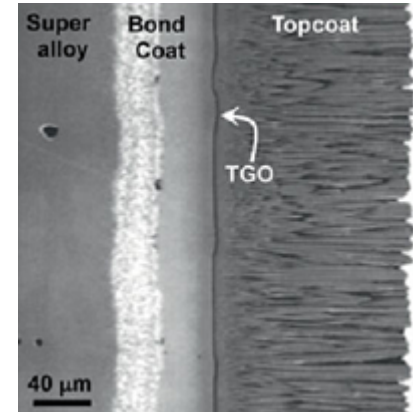
---

**Taishan Zhu, Dinkar Nandwana, Elif Ertekin**

Department of Mechanical Science & Engineering, University of Illinois

# Thermal Transport

## Why does it matter?

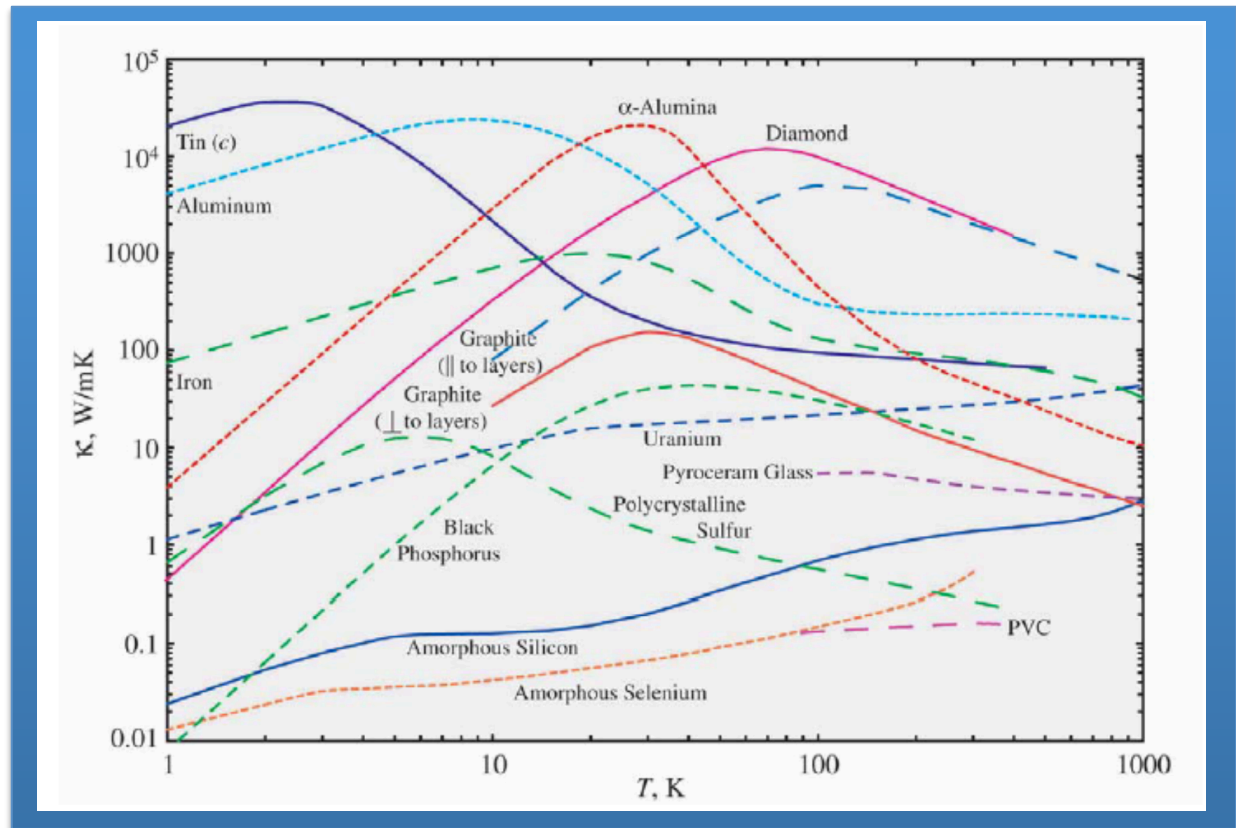


# Heat Transport in Solids

## Macroscale



*Thermal conductivity of typical solid materials:*



Temperature Gradient

$$Q = -k \nabla T$$

Heat current

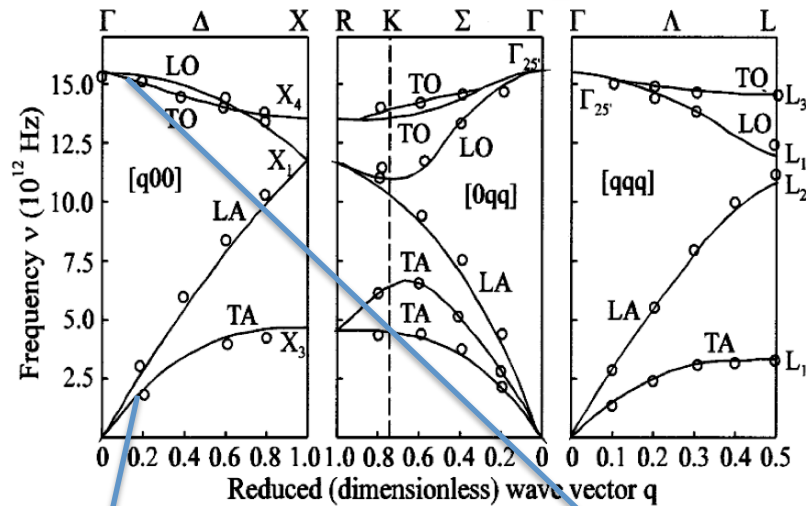
Thermal conductivity

# Heat Transport in Solids

## Atomic Scale

Mechanisms:

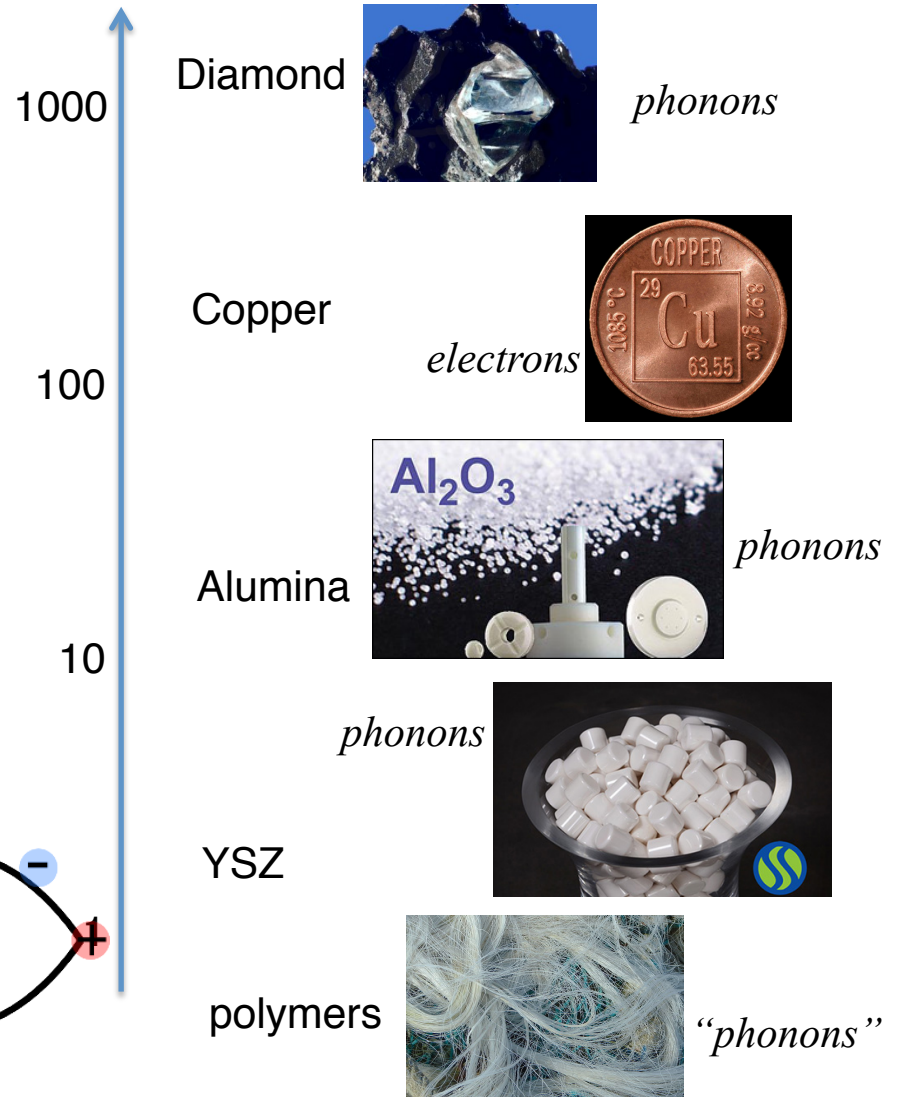
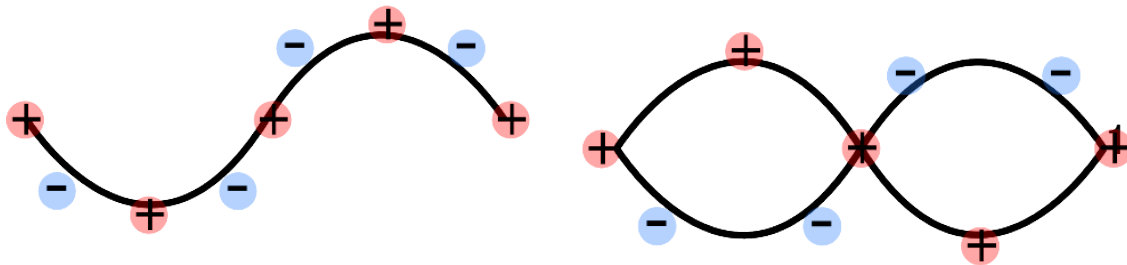
Phonons: quantized lattice vibrations



<http://www.ioffe.rssi.ru/SVA/NSM/Semicond/SiGe/mechanic.html>

Acoustical Mode

Optical Mode

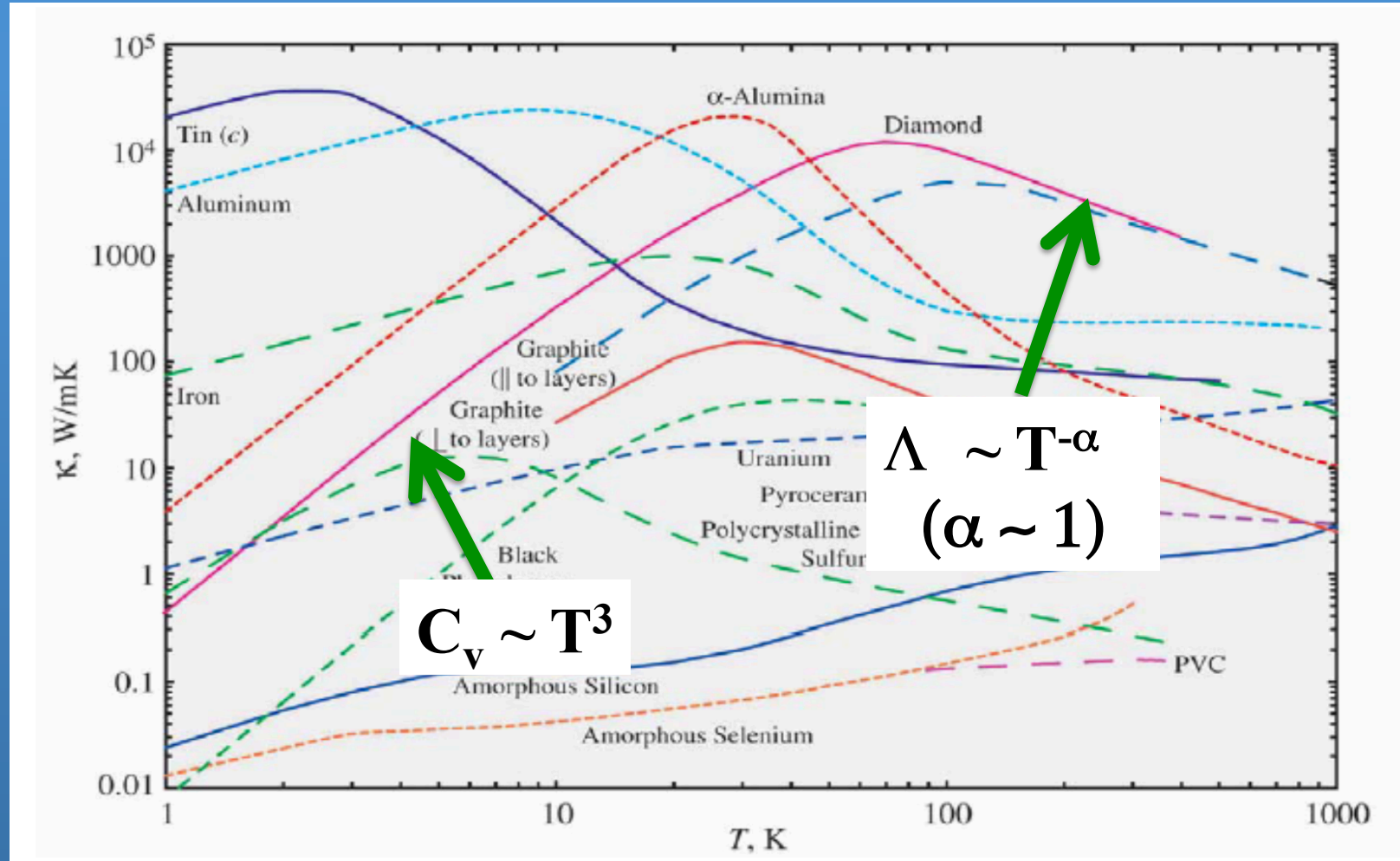




# Heat Transport in Nanostructures

In an infinite solid, scattering of phonons by other phonons, defects, and system boundaries limits the thermal conductivity of typical solid materials:

Thermal conductivity of typical solid materials:

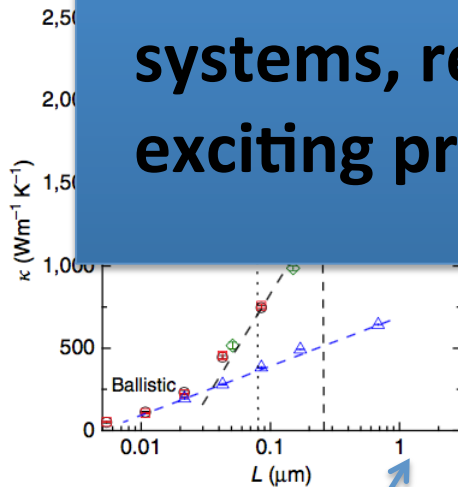
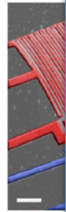


# Examples: Transport in Low Dimensions

Diverging thermal conductivity with length  
(controversial!)

$$\kappa = \int_0^{\omega_{\max}} \hbar \omega D(\omega) \frac{\partial f_{BE}}{\partial T} v_g^2 \tau d\omega$$

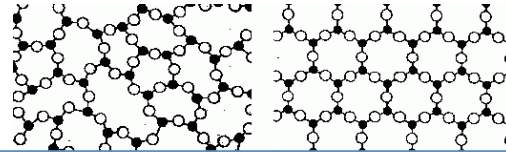
a



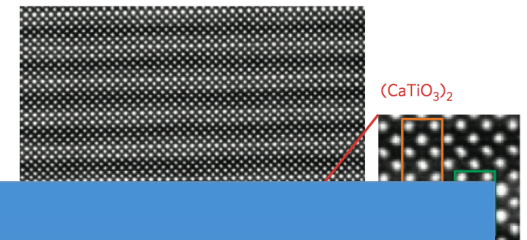
Note size of simulated system: 1 μm

*X. Xu et al., Nat Comm 5 3689 (2014)*

Interactions of Disorder and Low Dimensions



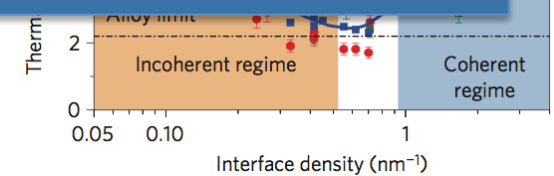
Nanostructured Devices



In all of these examples, the Blue Waters system has helped us to reveal new underlying physics in these nanostructured and/or low-dimensional systems, resolve existing controversies, and make exciting predictions!

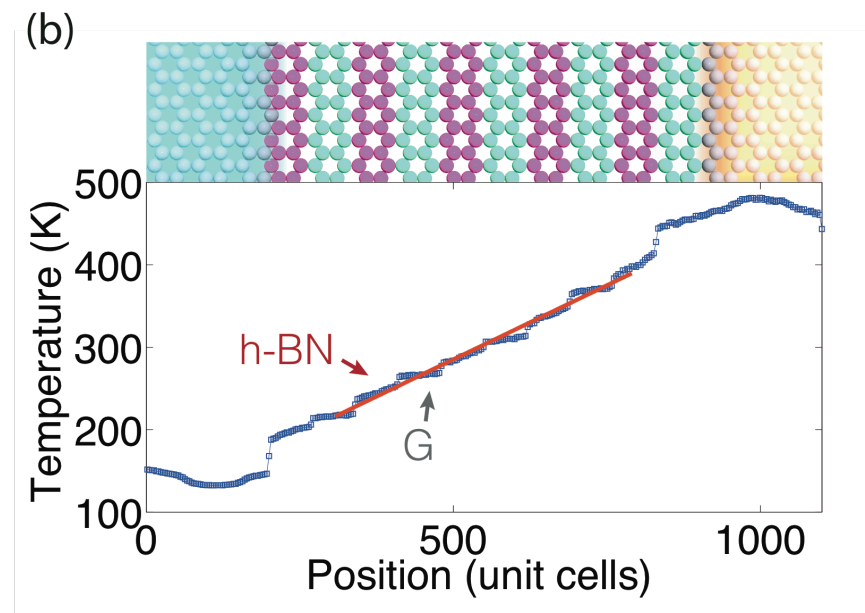
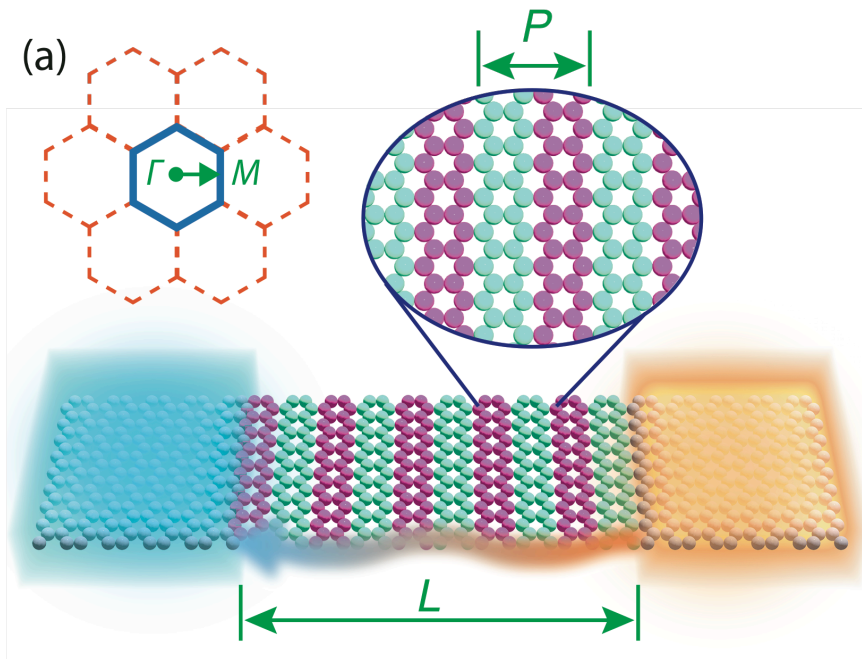
Diamond nanotreads with ordered & disordered SW defects

*Thomas C. Fitzgibbons, et al, Nat. Mater. 2015*

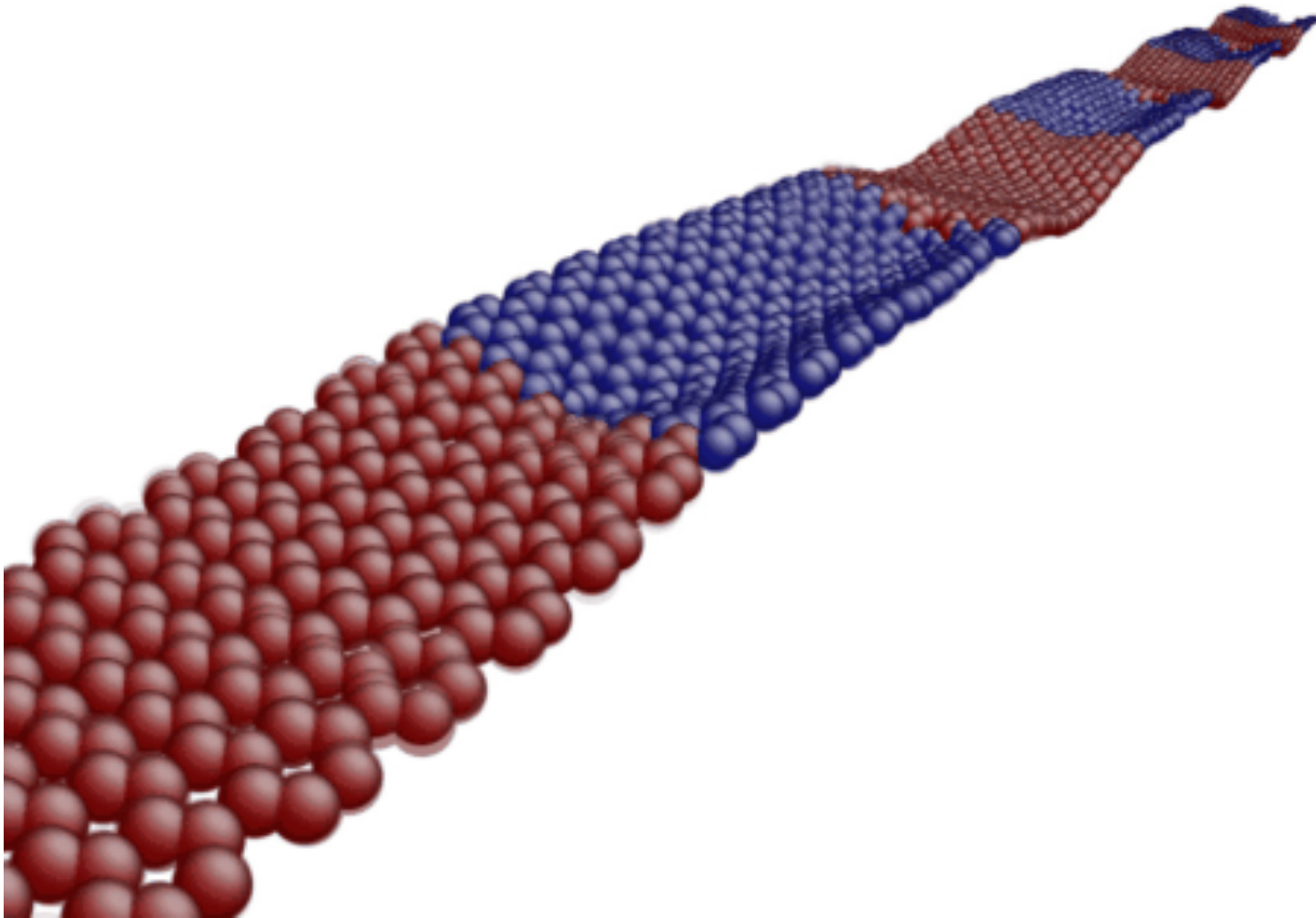


*Ravichandaran et al., Nat Materials 13 168 (2013)*

# Simulation Methodology

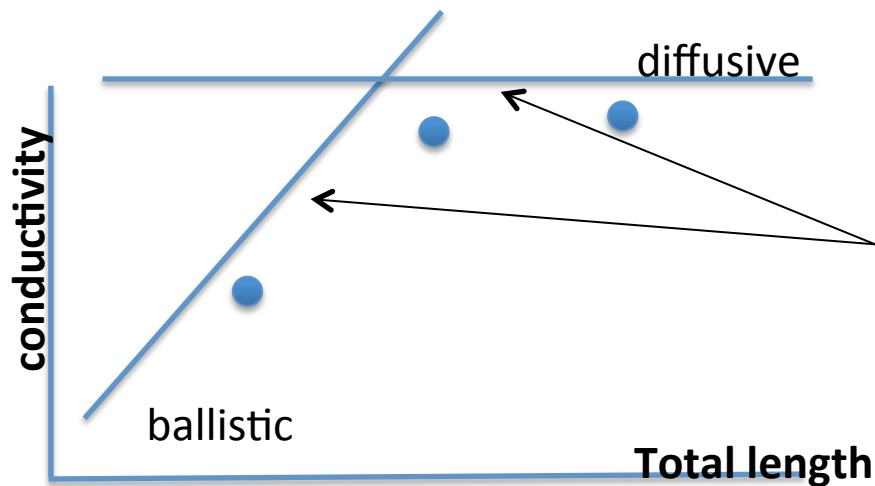


*approach: non-equilibrium molecular dynamics ... mimic reality!*

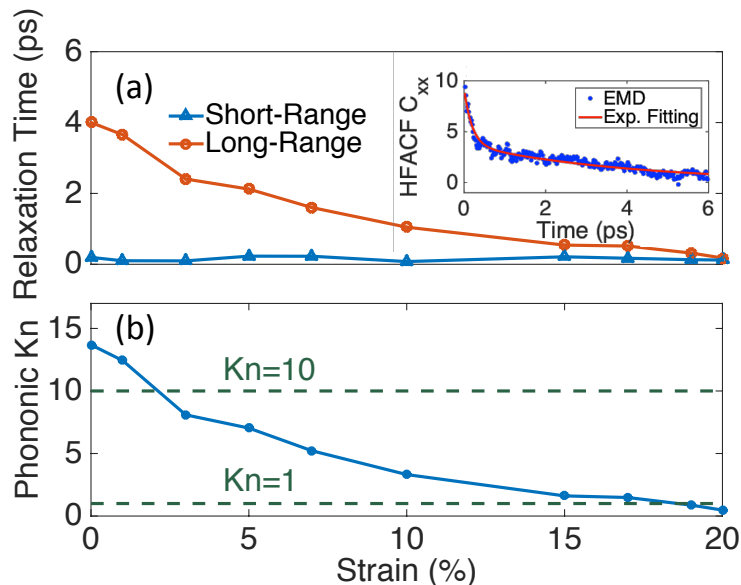




# Why Blue Waters? ... One example

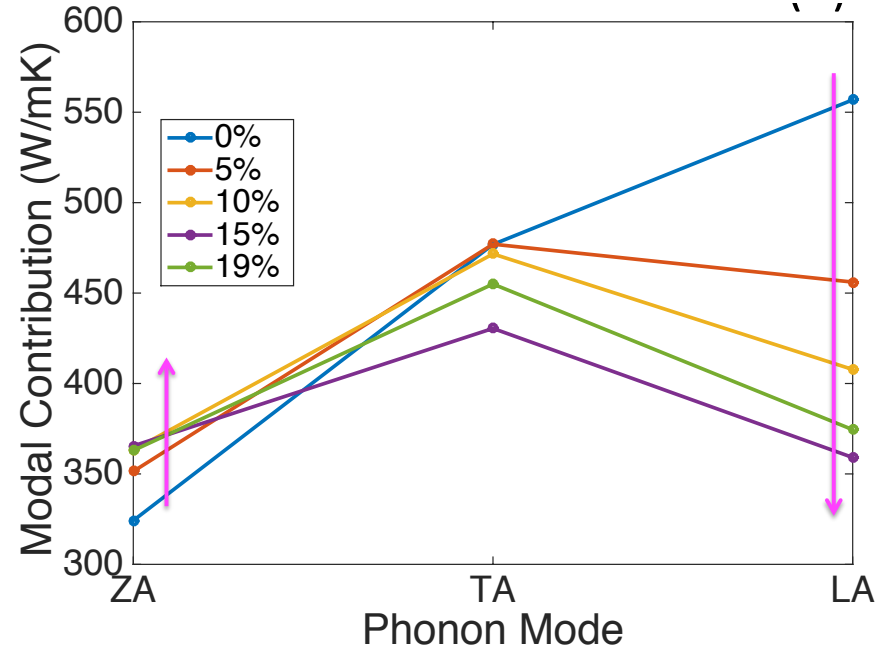
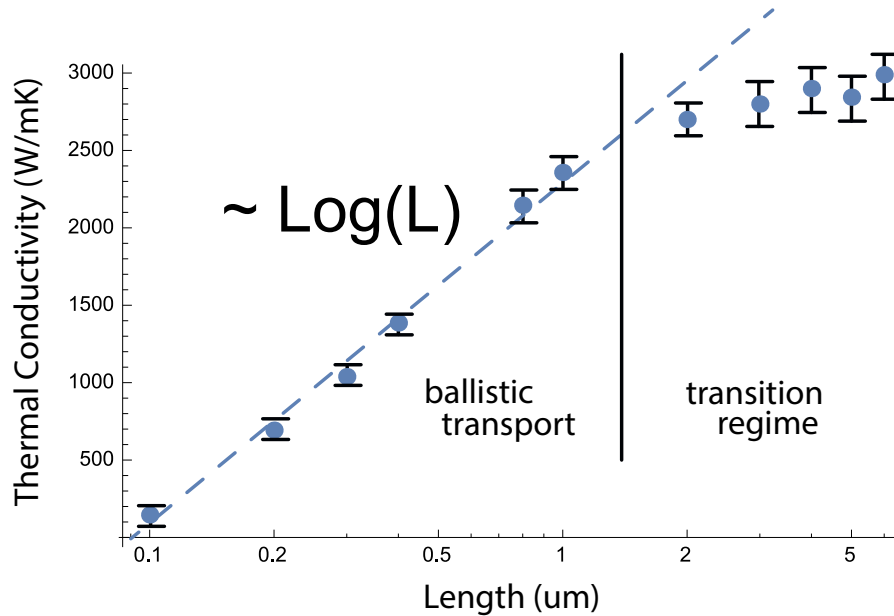


Length  $<$  Phonon Mean Free Path  
 Length  $>$  Phonon Mean Free Path



- Extract phonon mean free paths from the heat flux auto correlation function
- For the long ranged phonons, relaxation times around = 4 ps
- Mean free paths are around  $\Lambda = v_g \tau = 0.10 \mu\text{m}$
- **Purely diffusive transport regime should be visible around  $\text{Kn} = \Lambda/L = 0.01$ ,  $L = 10 \mu\text{m}$**

# Accomplishments - I



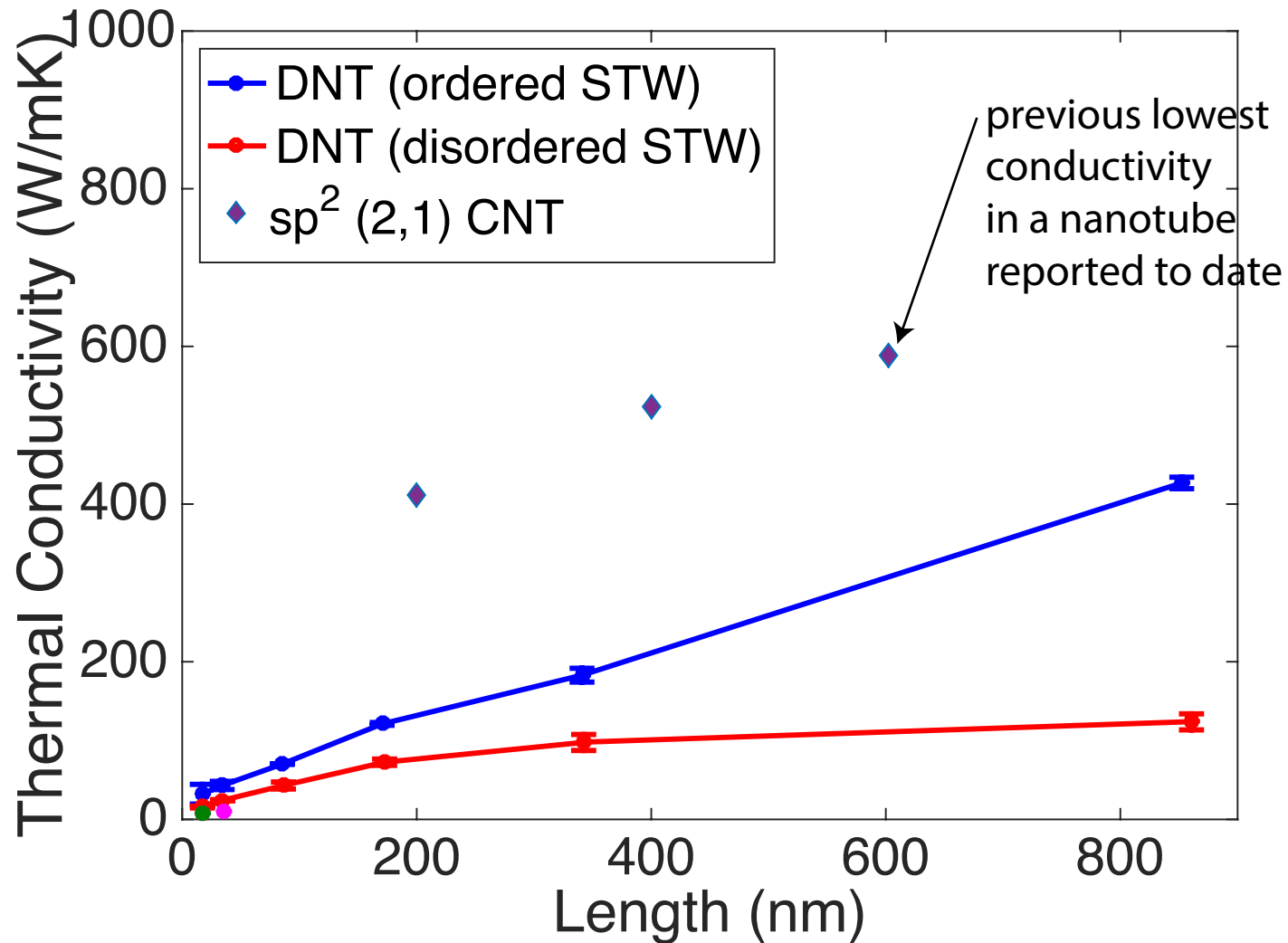
- Demonstration of transition from ballistic to transitional transport regime (required simulations of samples 2 – 6 μm side length! Largest to date.)
- Physical insight ... what did we learn? Why is the divergence suppressed?

# Accomplishments II – Disordered Systems

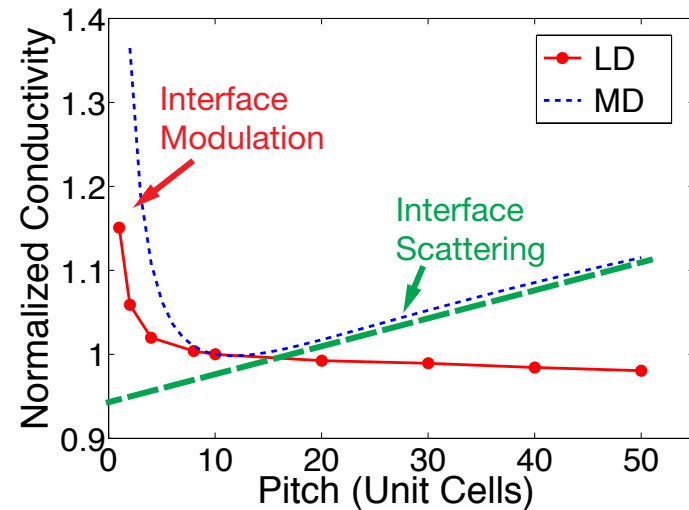
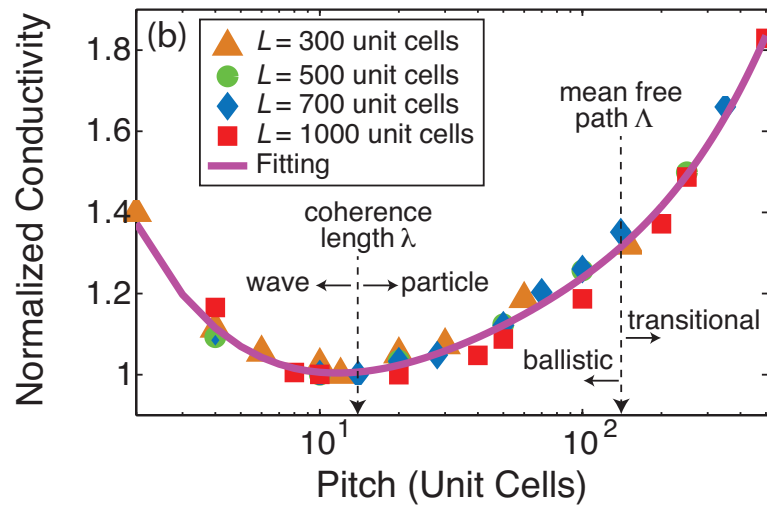
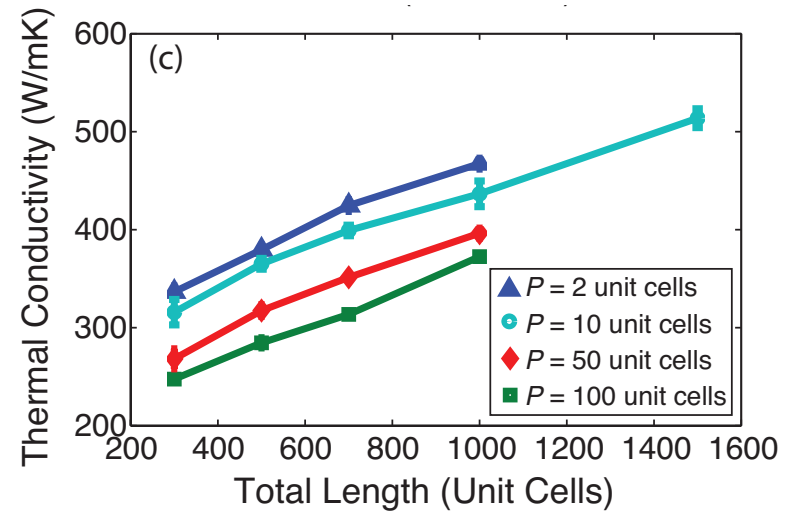
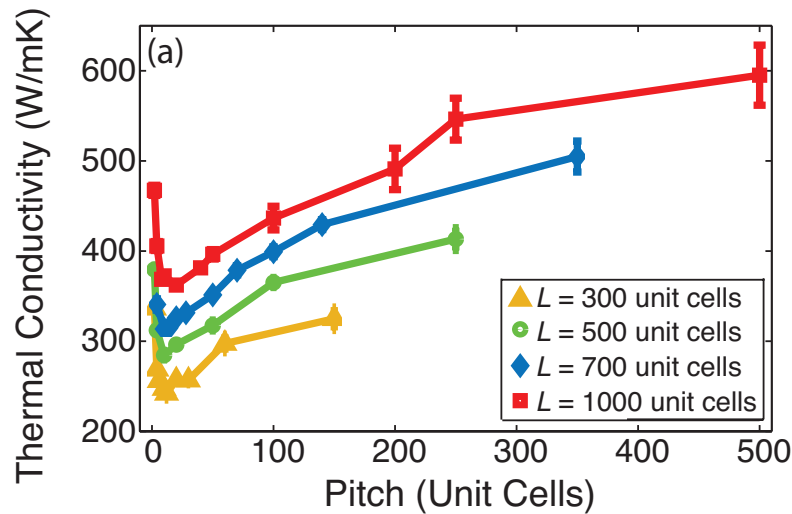
On one hand, the thermal conductivity of a 1D linear chain is other, transp

$sp^3$  (3,0) CNT

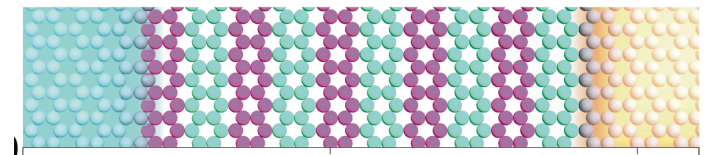
DNT with ordered & disordered SWs



# Accomplishments - III

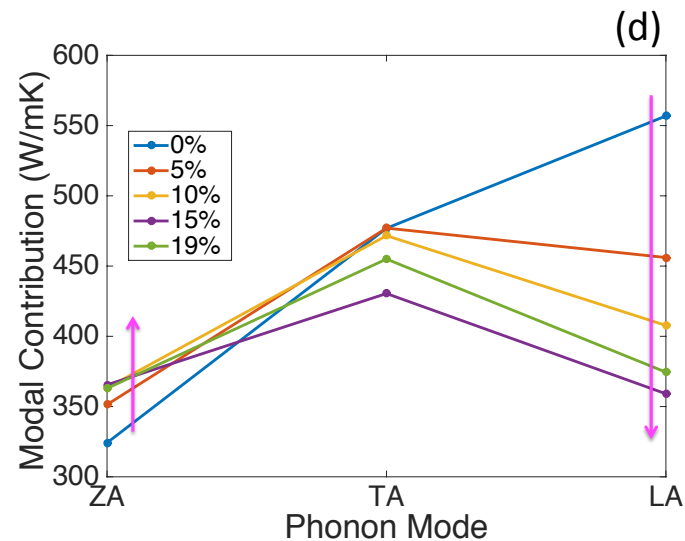
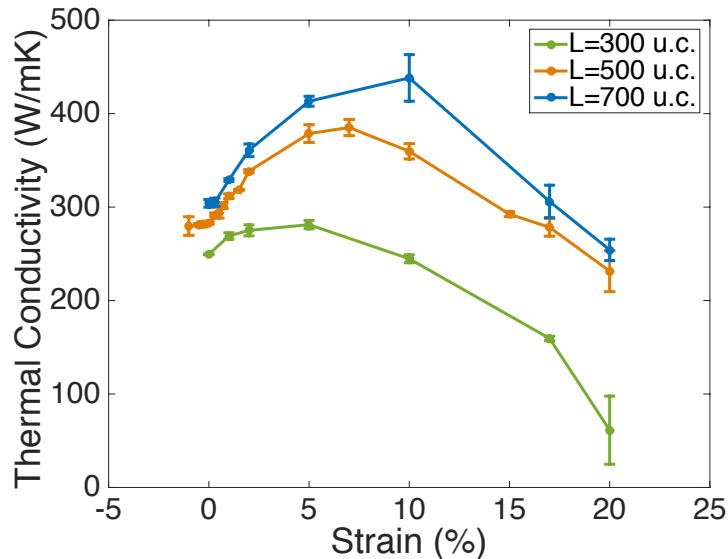
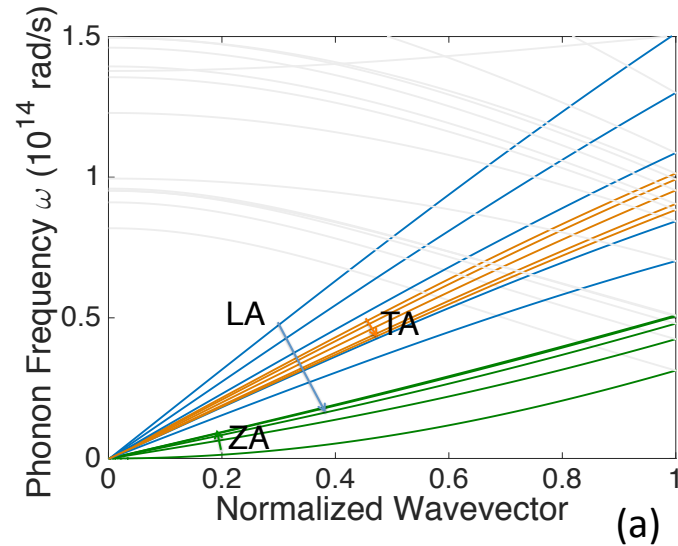
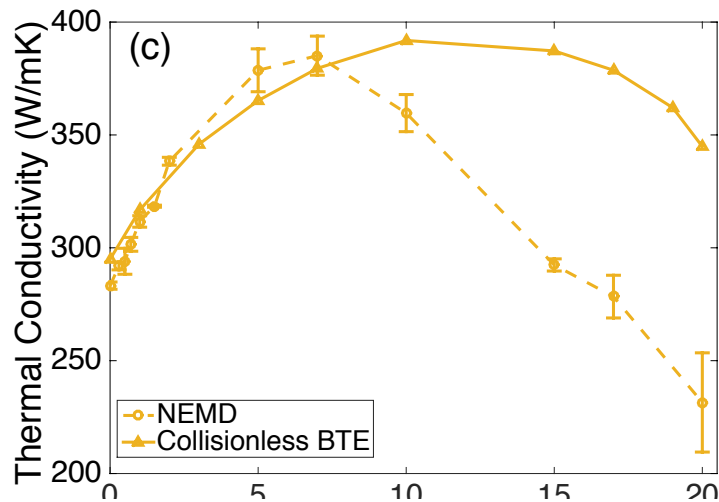


**Tuning the thermal conductivity by introducing superlattices into 2D materials**





# Accomplishments - IV



Conventional wisdom tells us that applying strain (in 3D solids) tends to reduce the thermal conductivity. What about in 2D? Anomalous, non-monotonic trends.

# Conclusions/Summary

- The Blue Waters system has enabled us to carry out large scale molecular dynamics simulations to reveal exciting new thermal transport physics in low-dimensional systems
- **Team contributions:** And, thank you to the Blue Waters team for their regular, timely help with our work!
- **References:**
  - T. Zhu, E. Ertekin. Phys. Rev. B 2014
  - T. Zhu, E. Ertekin. Phys. Rev. B 2015
  - D. Nandwana, E. Ertekin. Nano Lett. 2015
  - T. Zhu, E. Ertekin (submitted for publication)